

MAF
230 Homework #3 key

(1)

1. a. $f(x) = (2x+1)^2 = 4x^2 + 4x + 1$

$f'(x) = 8x + 4$

b. $(2x+1)(2x+1)$

$f'(x) = 2(2x+1) + 2(2x+1) = 4(2x+1) = 8x+4$

c. $(2x+1)^2$

$f'(x) = 2(2x+1) \cdot 2 = 4(2x+1) = 8x+4$

d. They are all the same

2. a. $(8 + \frac{1}{2\sqrt{x}})(5x^2 + 3) + (8x + \sqrt{x})(10x)$

b. $3(5x+2)^2(5)(2x-3)^8 + (5x+2)^3 8(2x-3)^7(2)$

c. $3x^2(6x+1)^2(7x-2)^4 + x^3(2)(6x+1)(6)(7x-2)^4 + x^3(6x+1)^2(4)(7x-2)(7)$

d. $(8x+3)e^{x^2-7x} + (4x^2+3x)e^{x^2-7x}(2x-7)$

e.
$$\frac{(\frac{1}{3}x^{-2/3})(\sqrt{x}+3) - (\sqrt[3]{x}-7)(\frac{1}{2}x^{-1/2})}{(\sqrt{x}+3)^2} = \frac{\frac{1}{3\sqrt[3]{x^2}}(\sqrt{x}+3) - (\sqrt[3]{x}-7)(\frac{1}{2\sqrt{x}})}{(\sqrt{x}+3)^2}$$

f.
$$\frac{1}{2} \left(\frac{x^2+x}{x^2-x} \right)^{-1/2} \left(\frac{(2x+1)(x^2-x) - (2x-1)(x^2+x)}{(x^2-x)^2} \right) = \frac{1}{2} \sqrt{\frac{x^2-x}{x^2+x}} \left[\frac{(2x+1)(x^2-x) - (2x-1)(x^2+x)}{(x^2-x)^2} \right]$$

g. $6(2x^3 + (4x-5)^2)^5(6x + 2(4x-5)(4))$